

Name: _____

Calculus I

– Formulas in a Nutshell –

Derivatives

- $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$
- Equation of Tangent Line to $f(x)$ at $x = a$:** $y - f(a) = f'(a)(x - a)$
- Constant Multiple:**
 $\frac{d}{dx}(cf(x)) = c \frac{d}{dx}f(x)$
- Sum/Difference Rule:**
 $\frac{d}{dx}(f(x) \pm g(x)) = \frac{d}{dx}f(x) \pm \frac{d}{dx}g(x)$
- Power Rule:**
 $\frac{d}{dx}(x^n) = nx^{n-1}$
- Product Rule:**
 $\frac{d}{dx}(f(x)g(x)) = f(x)\frac{d}{dx}g(x) + g(x)\frac{d}{dx}f(x)$
- Quotient Rule:**
 $\frac{d}{dx}\left(\frac{f(x)}{g(x)}\right) = \frac{g(x)\frac{d}{dx}f(x) - f(x)\frac{d}{dx}g(x)}{g(x)^2}$
- Chain Rule:**
 $\frac{d}{dx}(f(g(x))) = f'(g(x))\frac{d}{dx}g(x)$
- $\frac{d}{dx}(e^x) = e^x$
- $\frac{d}{dx}(a^x) = a^x \ln(a)$
- $\frac{d}{dx} \ln(x) = \frac{1}{x}$
- $\frac{d}{dx} \sin(x) = \cos(x)$
- $\frac{d}{dx} \cos(x) = -\sin(x)$
- $\frac{d}{dx} \tan(x) = \sec^2(x)$
- $\frac{d}{dx} \sec(x) = \sec(x)\tan(x)$
- $\frac{d}{dx} \csc(x) = -\csc(x)\cot(x)$
- $\frac{d}{dx} \cot(x) = -\csc^2(x)$
- $\frac{d}{dx} \arcsin(x) = \frac{1}{\sqrt{1-x^2}}$
- $\frac{d}{dx} \arccos(x) = \frac{-1}{\sqrt{1-x^2}}$
- $\frac{d}{dx} \arctan(x) = \frac{1}{1+x^2}$
- $\frac{d}{dx} \sinh(x) = \cosh(x)$
- $\frac{d}{dx} \cosh(x) = \sinh(x)$
- L'Hôpital's Rule:**
If f, g are differentiable and $f(a) = g(a) = 0$,
then $\lim_{x \rightarrow a} \frac{f(x)}{g(x)} = \lim_{x \rightarrow a} \frac{f'(x)}{g'(x)}$

Integrals

1. **Fundamental Theorem of Calculus:**

If f is continuous on $[a, b]$ and $f(t) = F'(t)$,
then $\int_a^b f(t)dt = \underline{\hspace{2cm}}$

2. $\int_a^b f(x)dx = - \int_{\underline{\hspace{1cm}}}^{\underline{\hspace{1cm}}} \underline{\hspace{1cm}}$

3. $\int_a^c f(x)dx + \int_c^b f(x)dx = \underline{\hspace{2cm}}$

4. **Constant Multiple:**

$$\int_a^b cf(x)dx = \underline{\hspace{2cm}}$$

5. **Sum/Difference Rule:**

$$\int_a^b (f(x) \pm g(x)) dx = \underline{\hspace{2cm}}$$

6. **Average Value of f from a to b :**

$\underline{\hspace{2cm}}$

7. **Power Rule:**

$$\int x^n dx = \underline{\hspace{2cm}}, \text{ if } n \neq \underline{\hspace{1cm}}$$

8. **Constant Multiple:**

$$\int cf(x)dx = \underline{\hspace{2cm}}$$

9. **Sum/Difference Rule:**

$$\int (f(x) \pm g(x)) dx = \underline{\hspace{2cm}}$$

10. $\int \frac{1}{x} dx = \underline{\hspace{2cm}}$

11. $\int e^x dx = \underline{\hspace{2cm}}$

12. $\int \sin(x) dx = \underline{\hspace{2cm}}$

13. $\int \cos(x) dx = \underline{\hspace{2cm}}$