

**CENTRO DE INVESTIGACIONES  
EN OPTICA, A.C.**

**Diode semiconductor laser under external optical injection:  
Theory and Experiments**

**Brenda Esmeralda Martínez Zérega  
A. Pisarchik, M. Saucedo, R. Reategui and J. Liu**

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UC-MEXUS

# Outline

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A. Introduction

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B. Theory

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B. Theory

C. Experiments

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B. Theory

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D. Results

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A. Introduction

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## A. Introduction

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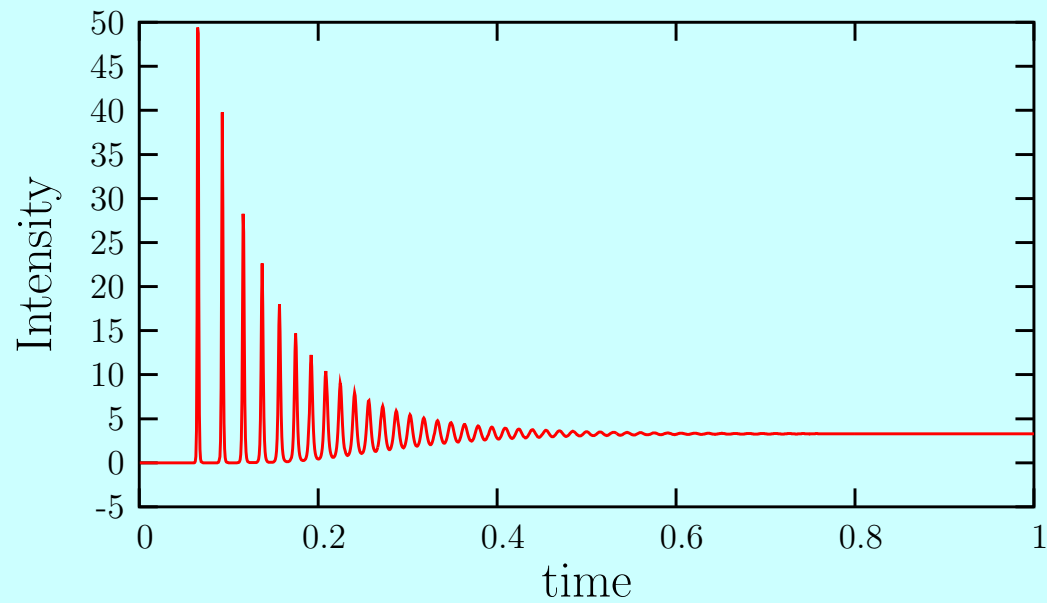
The relevant variables: field, population and polarization, decay on very different time scales given by the relaxation rates.

- **Class A:** Population and polarization decay fast in comparison with the field.  
Constant output solution
- **Class C:** Relaxation rates of the same magnitude.  
Undamped periodic or no-periodic (chaotic) pulsing.
- **Class B:** Only the polarization relaxes fast.  
Relaxation oscillations

## A. Introduction

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### Relaxation oscillation frequency-maximum gain frequency



Diode laser:  $f_r$  (GHz)  $\approx f_o$

## A. Introduction

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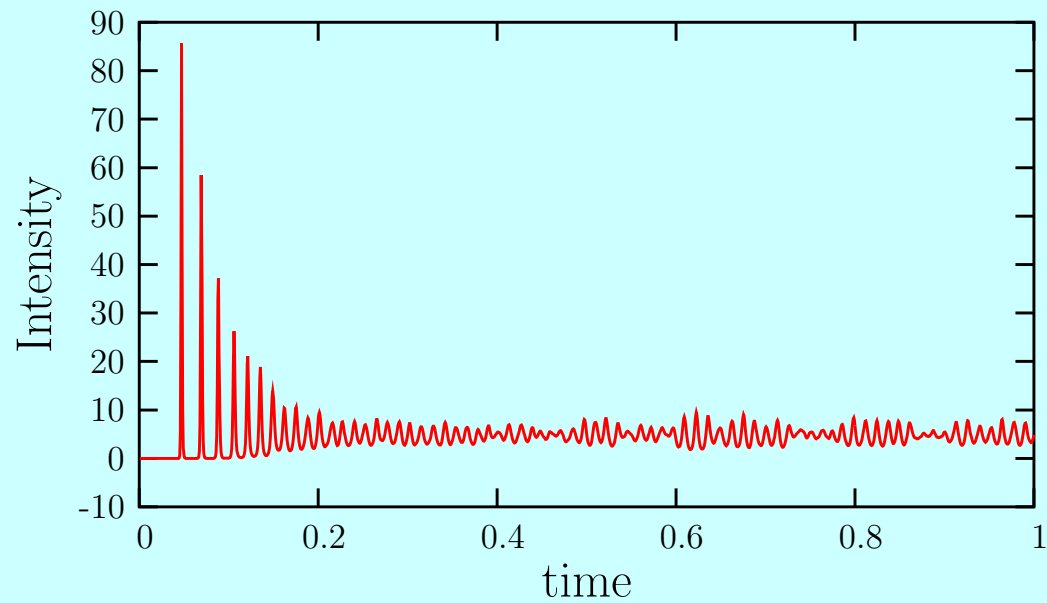
To add a degree of freedom

- Feedback
- Modulation
- Optical injection  
 $f_r = f_M - f_S$

## A. Introduction

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### Chaotic oscillations

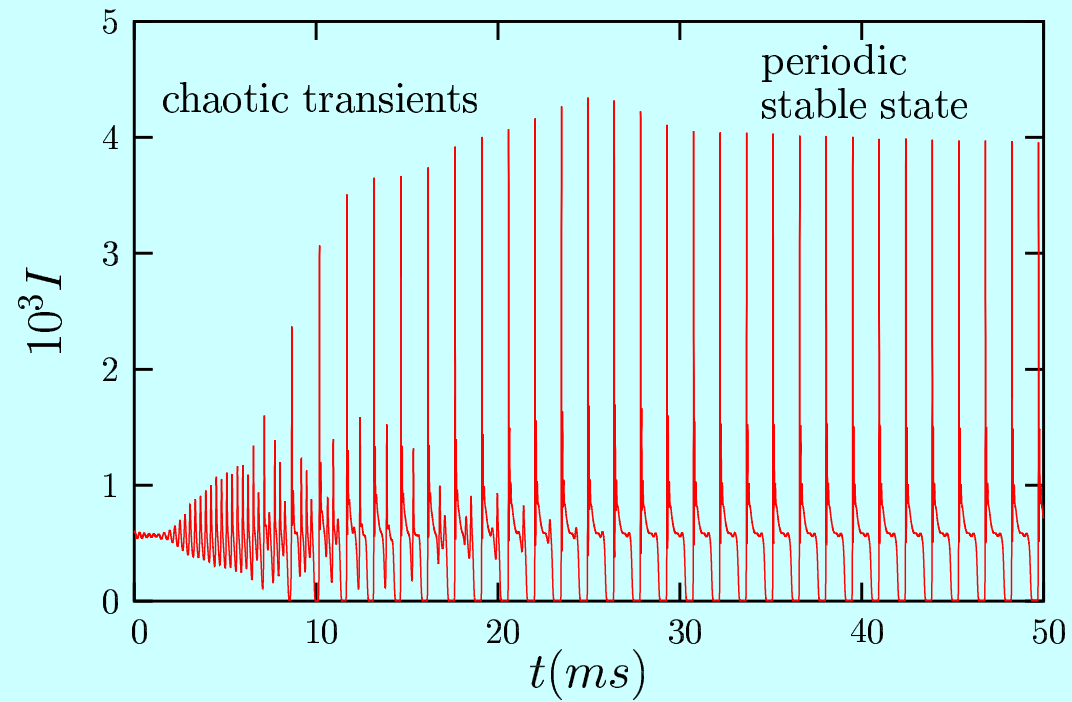


Diode laser:  $f_r$  (GHz)  $\approx f_o$

## A. Introduction

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### Undamped periodic oscillations for a class B laser



## B. Theory

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### Model equations

$$\frac{da}{d\tau} = \frac{1}{2}[\hat{\gamma}_d \hat{n} - \hat{\gamma}_n(2a + a^2)](1 + a) + \xi \cos(\hat{\Omega}\tau + \phi) + F_a$$

$$\frac{d\phi}{d\tau} = -\frac{\xi}{1+a} \sin(\hat{\Omega}\tau + \phi) + \frac{F_\phi}{1+a} - \frac{b}{2}[\hat{\gamma}_d \hat{n} - \mu \hat{\gamma}_n(2a + a^2)]$$

$$\frac{dn}{d\tau} = -[\hat{\gamma}_d \hat{n} - \hat{\gamma}_n(2a + a^2)](1 + a)^2 + \hat{\gamma}_s \hat{n} - (2a + a^2)$$

$a$  is the slave laser normalized field amplitude,  
 $\phi$  is the phase difference between master and slave fields,  
 $n$  is the slave normalized carrier density,  
 $\gamma_s$  spontaneous carrier relaxation rate,  
 $\gamma_d$  differential carrier relaxation rate,  
 $\gamma_n$  nonlinear carrier relaxation rate,  
 $b$  is the linewidth enhancement factor,  
 $\xi$  is the injection parameter,  
 $f = \Omega/2\pi$  is the frequency detuning,  
 $\tau = t\gamma_c$  represents the normalized time,  
 $\mu$  is the nonlinear gain effect (0 or 1),  
 $F_{phi}$  and  $F_a$  are noise terms,

## B. Model Equations

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### Laser parameters

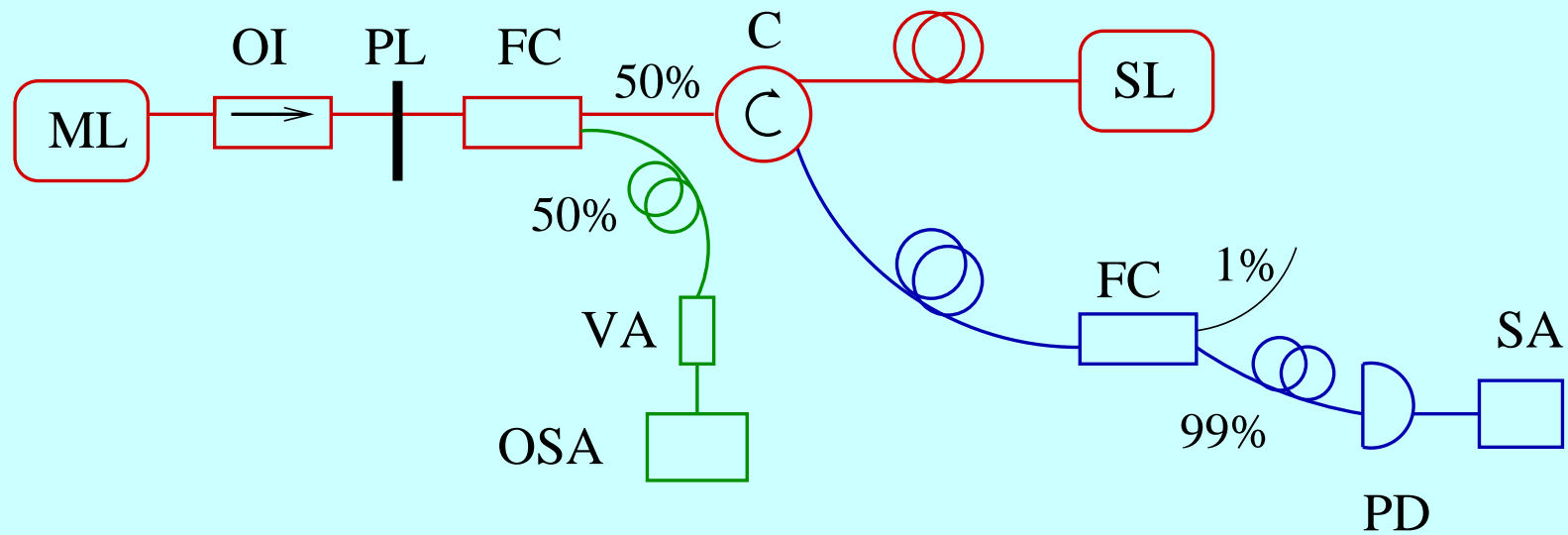
$J$	$b$	$\hat{\gamma}_c$
4.0	6.0	$5.0 \times 10^{11} \text{s}^{-1}$
$\gamma_s / \gamma_c$	$\hat{\gamma}_d$	$\hat{\gamma}_n$
$6.92 \times 10^{-3}$	$4.23 \times 10^{-3} J$	$9.6075 \times 10^{-3} J$

$J$  is the injection current

$\gamma_c$  is the cavity decay rate

## C. Experiments

### Experimental setup



Fixed slave operating parameters

$$\lambda_s = 1535.454\text{nm}$$

$$T_s = 20^\circ\text{C}$$

$$I_s = 20\text{mA}$$

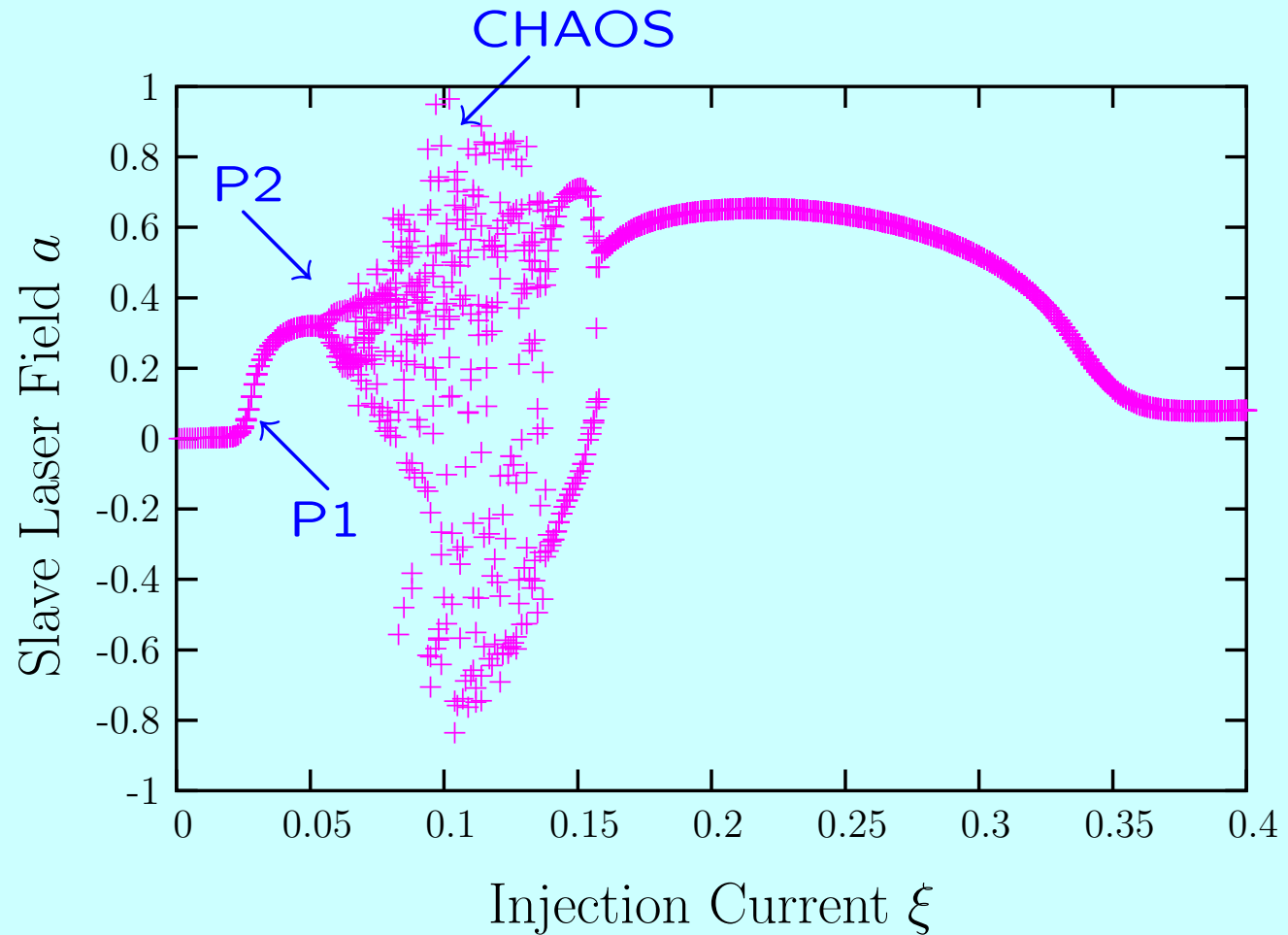
Detuning frequency is defined as

$$f_D = f_M - f_S$$

## C. Results

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### Bifurcation Diagram

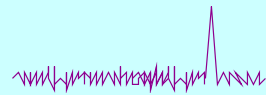
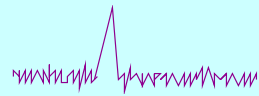
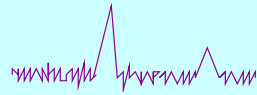
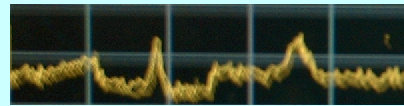
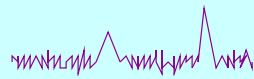
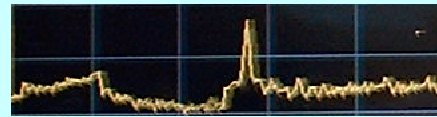
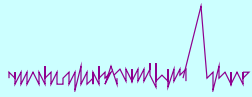


1975 Feigenbaum - Period-2 route to chaos Logistic map

# D. Results

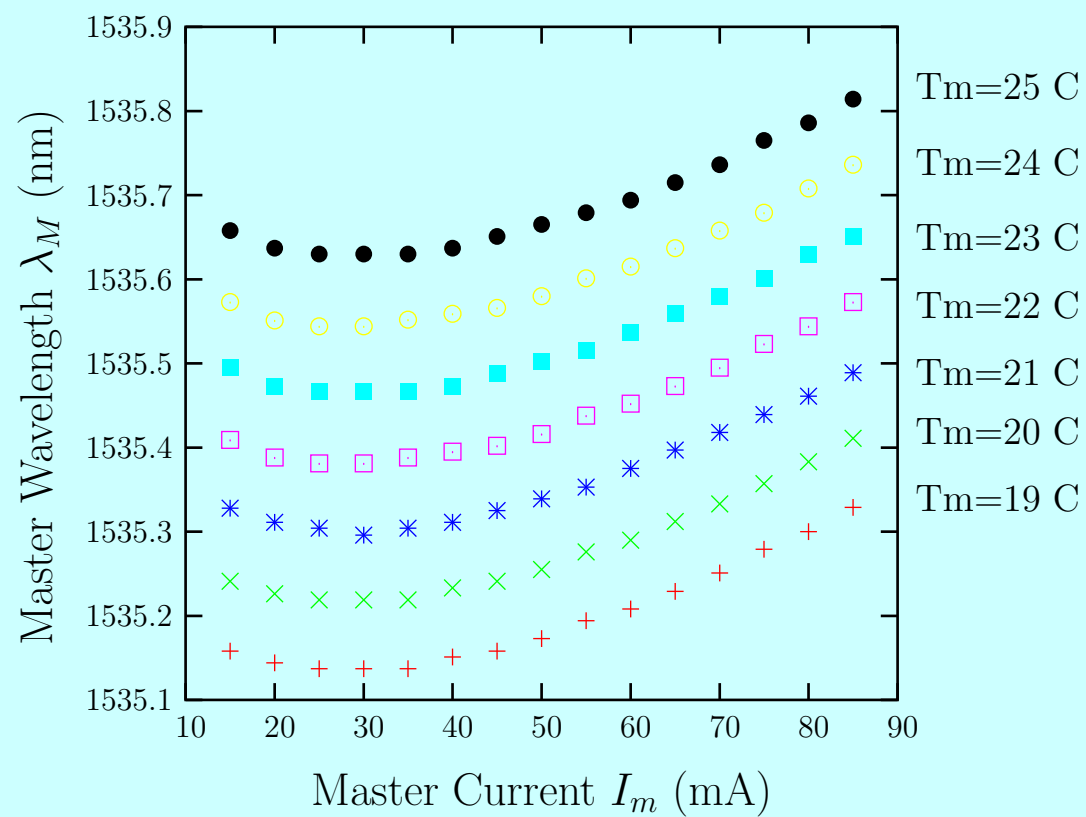
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## Spectrum

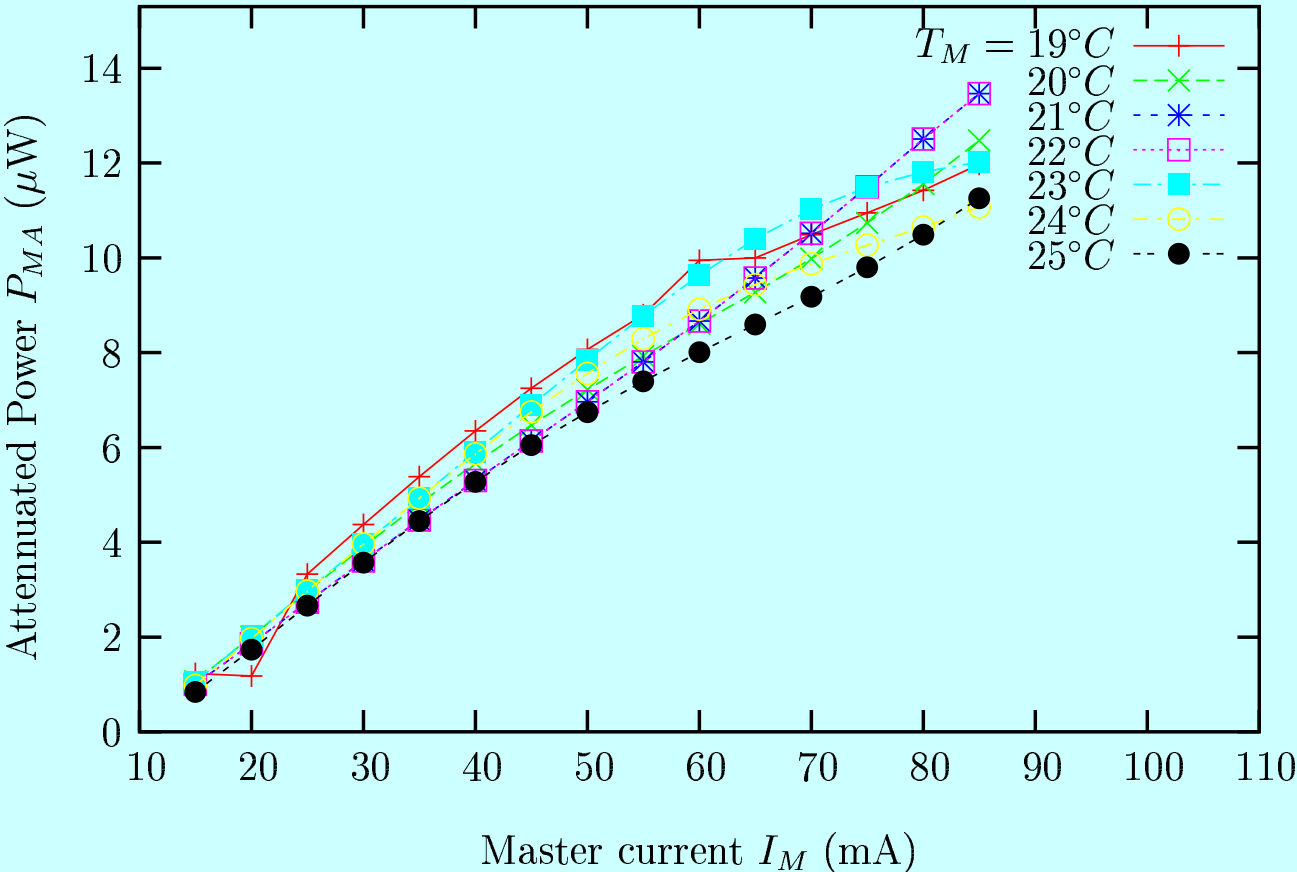


## D. Results

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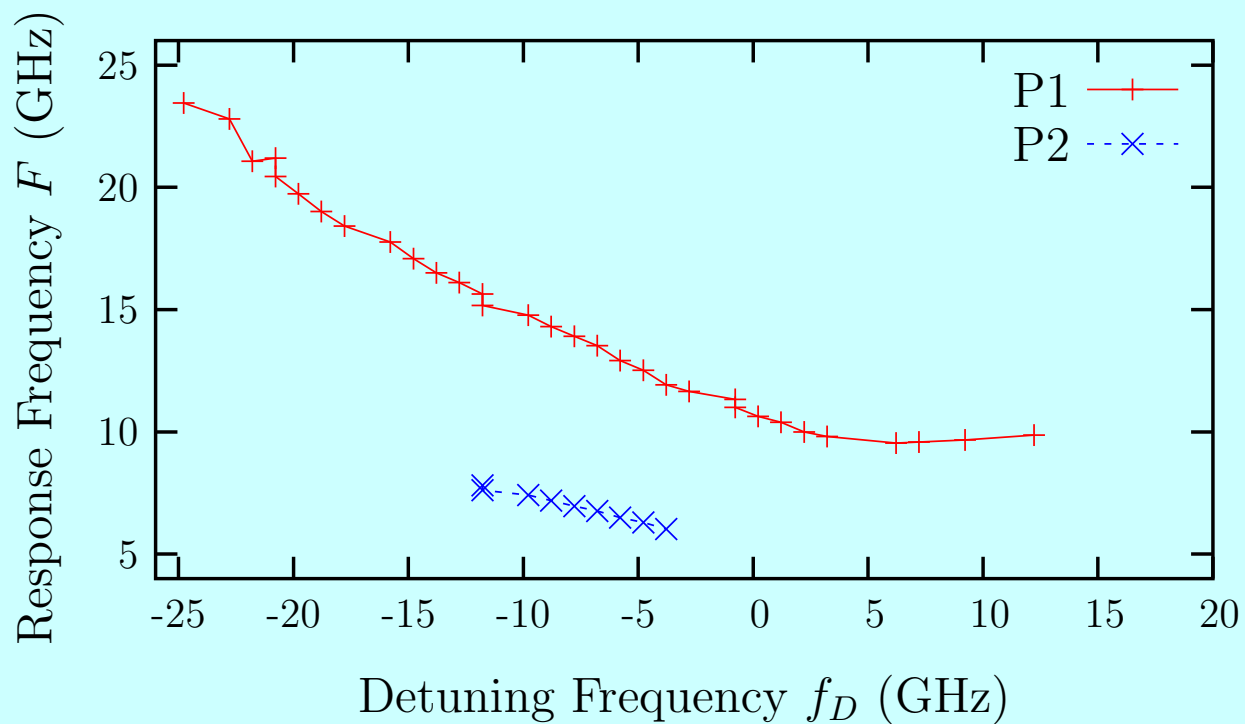
# D. Results



## D. Results

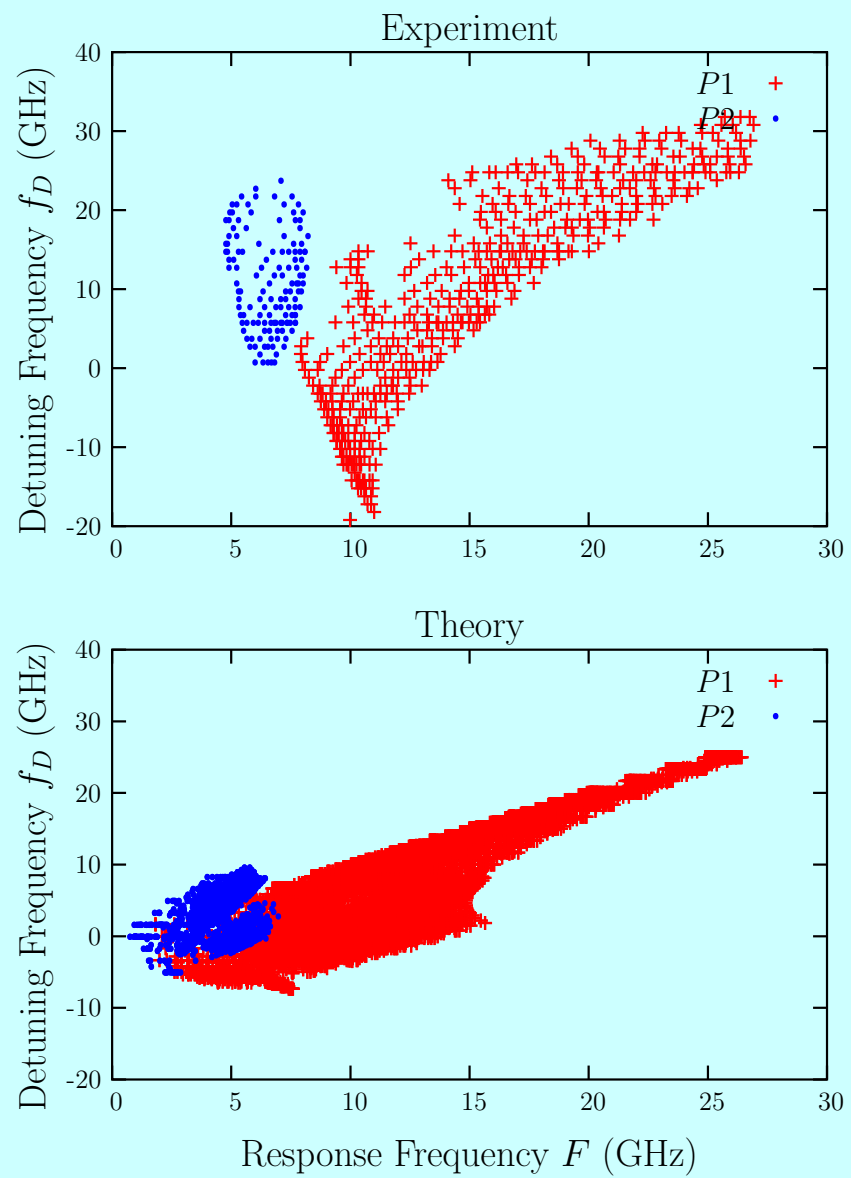
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$$I_M = 65mA$$



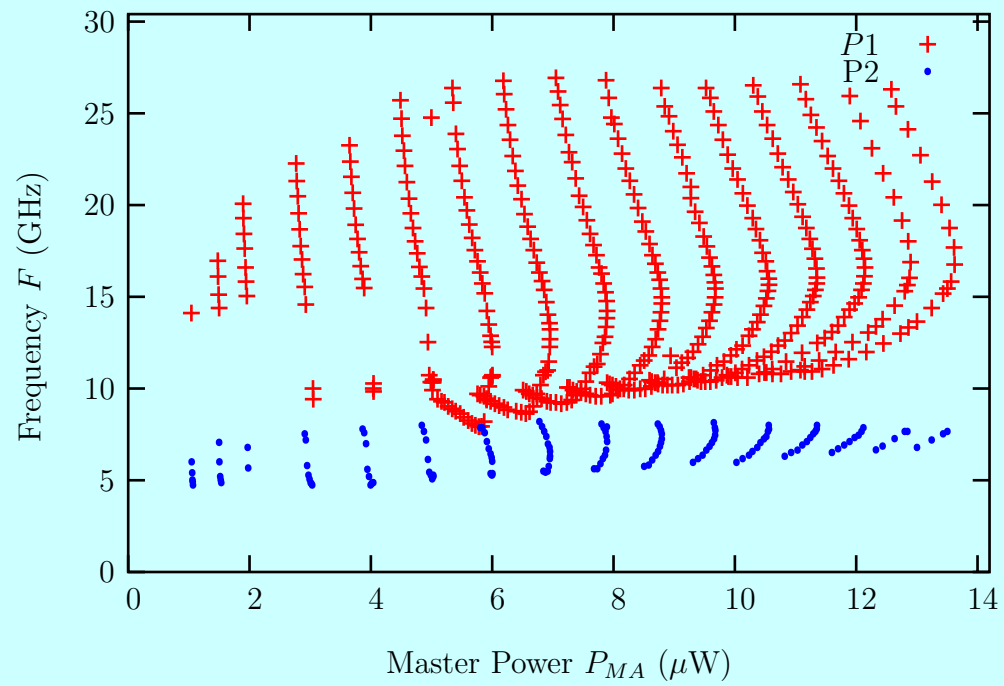
## D. Results

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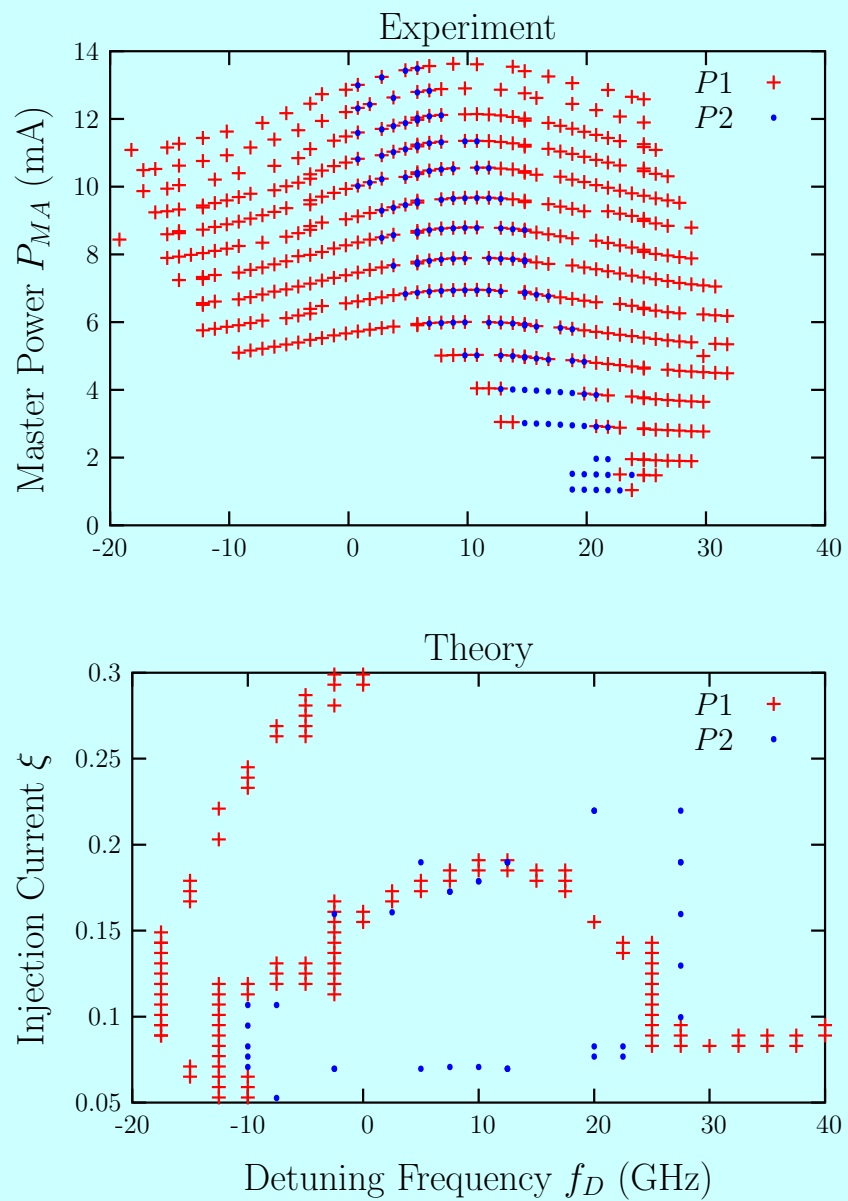
## D. Results

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## D. Results

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## E. Conclusions

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- We present theoretical and experimental evidence that optical injected diode lasers shows period-1 and period-2 oscillations.
- First we studied the master output power and its optical frequency (wavelength) dependence on temperature and current variations.
- We sampled the spectra of an optically injected diode laser as the injection power was increased.

- The changes in the frequency separation between the principal oscillations were studied as a function of the detuning frequency and the injection power.
- We found qualitative agreement between theory and experiments.
- We believe that our results can be useful to understand period-one oscillations in optically injected semiconductor lasers as a function of some parameter that are accessible for the experimental point of view.
- We believe that high period oscillations may be lost in our experiment by the peaks becoming too small.
- Still a lot work to do in order to understand the dynamics!

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Thank you!