

$$\lambda_* \sim R(S \log S)^{-1/3}$$