

$$\chi \equiv R/l_* \sim R(S \log S)^{-1/3}$$