

- 16) a) True  
 b) False  
 c) True  
 d) True  
 e) True  
 f) True  
 g) False  
 h) False

17)  $x > \frac{11}{2}$

- 18) Yes it's possible. The remaining eigenspace could be 1-dimensional. But the union of the bases of the eigenspaces must have 7 vectors in order for the matrix to be diagonalizable.

- 19) Find a diagonal matrix that A is similar to.  $D_1$   
 " " " " that B is similar to  $D_2$ .  
 If  $D_1 = D_2$  then  $A \sim B$ .

- 20) a)  $\lambda = 3, -1 \Leftrightarrow k = 3$ .  
 b)  $\lambda = 1$  with mult 2  $\Leftrightarrow k = -1$ .  
 c) A has no real eigenvalues  $\Leftrightarrow k < -1$ .

- 21) Addition is not associative  
 There is no zero or additive inverse  
 $1 \cdot x \neq x$ .  
 $c_1(c_2x) \neq (c_1c_2)x$ .  
 distributivity doesn't hold.

- 22)  $W_1 = \left\{ \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix} \right\}$   $W_2 = \left\{ \begin{bmatrix} a \\ 0 \\ 2 \end{bmatrix} \right\}$   
 $W_1 \cup W_2 = \left\{ v \in \mathbb{R}^3 : v = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix} \text{ or } v = \begin{bmatrix} a \\ 0 \\ 2 \end{bmatrix} \right\}$   
 but the sum of these two vectors is not in  $W_1 \cup W_2$ , so  
 $W_1 \cup W_2$  is not a subspace of  $\mathbb{R}^3$ .