

1. **Estimating population mean  $\mu$  with the assumption that  $\sigma$  is known (Normal distribution):**

- **Confidence interval:**

$$\bar{x} \pm z^* \frac{\sigma}{\sqrt{n}}$$

Table *C* gives  $z^*$  for a given  $C\%$  confidence level.

- **Significance tests for the null hypothesis  $H_0 : \mu = \mu_0$ :**

The one sample  $z$  test statistic:

$$z = \frac{\bar{x} - \mu_0}{\sigma/\sqrt{n}}$$

Find the  $P$ -value of  $z$  using Table A, do some algebra depending on your alternative hypothesis  $H_a$ .

2. **Estimating population mean  $\mu$  with the assumption that  $\sigma$  is not known (t distribution):**

- **The one sample  $t$  confidence interval:**

$$\bar{x} \pm t^* \frac{s}{\sqrt{n}}$$

Table *C* gives  $t^*$  for a given  $C\%$  confidence level and  $df = n - 1$ .

- **One sample significance tests for the null hypothesis  $H_0 : \mu = \mu_0$ :**

The one sample  $t$  statistic

$$t = \frac{\bar{x} - \mu_0}{s/\sqrt{n}}, \text{ with } df = n - 1$$

Find the  $P$ -value of  $t$  using Table C with  $df = n - 1$ , take in consideration whether you have a one sided or two sided alternative hypothesis.

- **Matched pairs:** Use the above one sample procedures to analyze matched pairs by taking the difference within each matched pair to produce a single sample.

3. **Comparing two population means  $\mu_1$  and  $\mu_2$  with the assumption that  $\sigma_1$  and  $\sigma_2$  are not known (t distribution):**

- **The two sample  $t$  confidence interval:**

$$\bar{x}_1 - \bar{x}_2 \pm t^* \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$$

Table *C* gives  $t^*$  for a given  $C\%$  confidence level and  $df = \min(n_1 - 1, n_2 - 1)$ .

- **Two sample significance tests for the null hypothesis  $H_0 : \mu_1 = \mu_2$ :**

The two sample  $t$  statistic

$$t = \frac{\bar{x}_1 - \bar{x}_2}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}, \text{ with } df = \min(n_1 - 1, n_2 - 1)$$

Find the  $P$ -value of  $t$  using Table C, take in consideration whether you have a one sided or two sided alternative hypothesis.

4. **Estimating population proportion from a sample proportion  $\hat{p}$  (Normal distribution):**

- **Large sample confidence interval for a population proportion**

$$\hat{p} \pm z^* \sqrt{\frac{\hat{p}(1 - \hat{p})}{n}}$$

- **Significance test for proportion**

The  $z$  test statistic for the null hypothesis  $H_0 : p = p_0$  is

$$z = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0(1-p_0)}{n}}}$$

5. **Comparing two proportions**

- **The two sample  $t$  confidence interval for  $p_1 - p_2$ :**

$$\hat{p}_1 - \hat{p}_2 \pm z^* \sqrt{\frac{\hat{p}_1(1 - \hat{p}_1)}{n_1} + \frac{\hat{p}_2(1 - \hat{p}_2)}{n_2}}$$

- **Two sample significance tests for  $H_0 : p_1 = p_2$ :**

Use the pooled sample proportion

$$\hat{p} = \frac{\text{number of successes in both samples combined}}{\text{number of individuals in both samples combined}}$$

Then the  $z$ -statistic is

$$z = \frac{\hat{p}_1 - \hat{p}_2}{\sqrt{\hat{p}(1 - \hat{p})\left(\frac{1}{n_1} + \frac{1}{n_2}\right)}}$$