

Imaging Science

Israel J. Vaughn

Advanced Sensing Laboratory
College of Optical Sciences
University of Arizona



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Some personal info

- ▶ B.S. in Math

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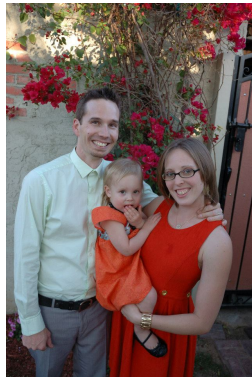
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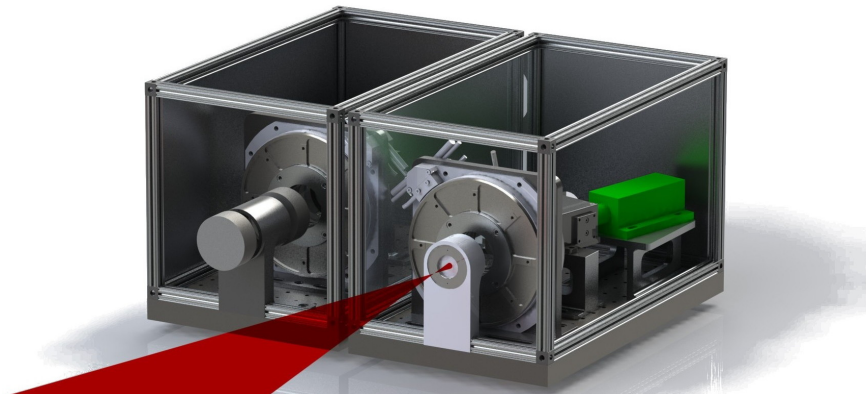


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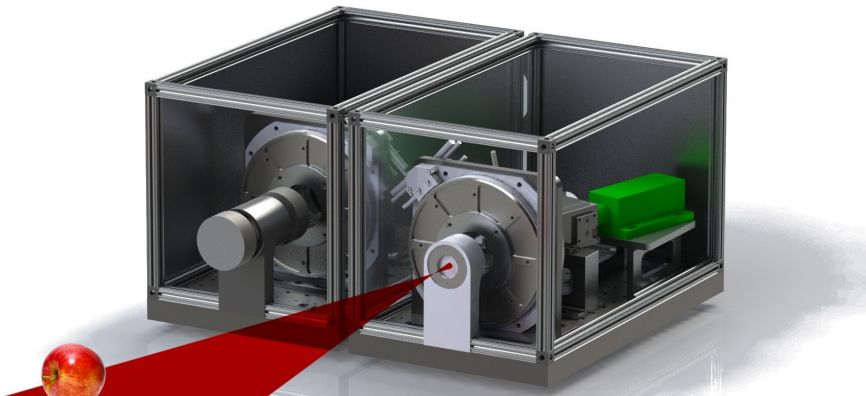


Mathematical model



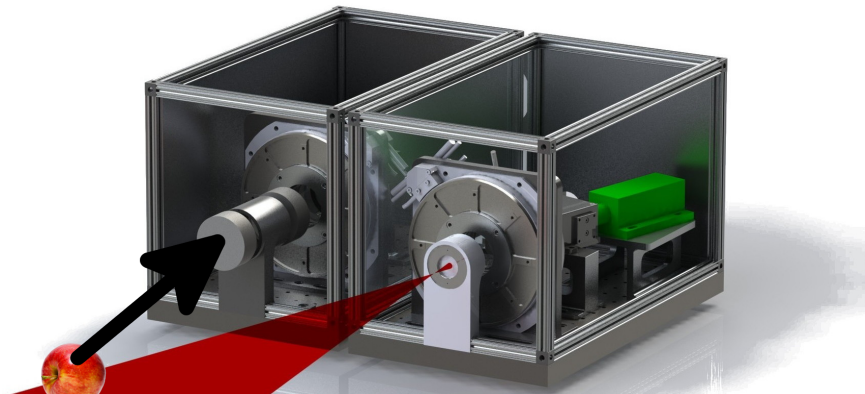
Mathematical model

- Begin with the physics (object)...



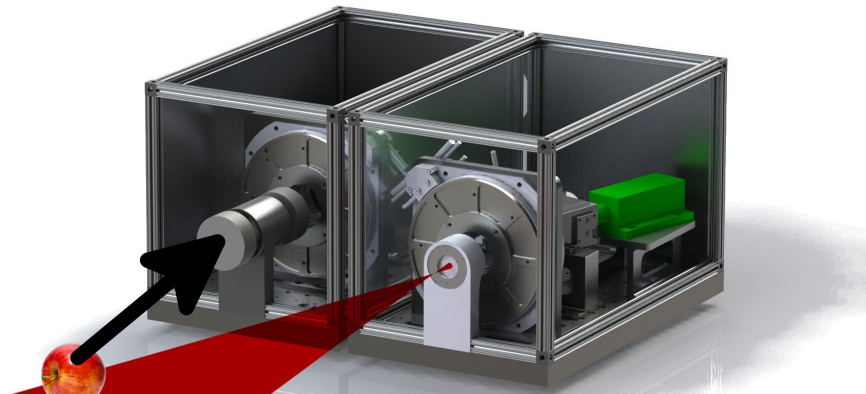
Mathematical model

- ▶ Begin with the physics (object)...
- ▶ Analyze physical interaction with an instrument to measured data (image)...



Mathematical model

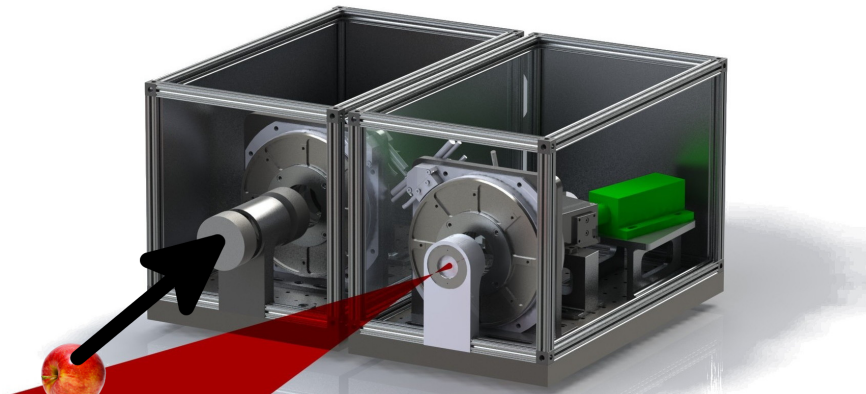
- ▶ Begin with the physics (object)...
- ▶ Analyze physical interaction with an instrument to measured data (image)...
- ▶ Derive a mathematical model from the physics and the physical interaction.



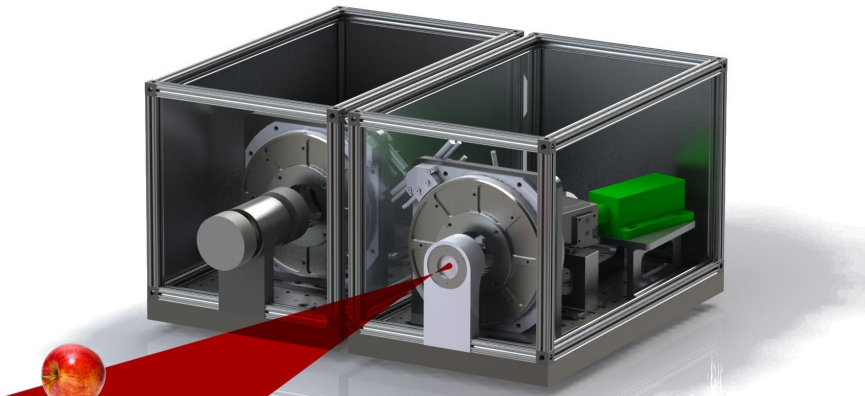
Mathematical model

- ▶ Begin with the physics (object)...
- ▶ Analyze physical interaction with an instrument to measured data (image)...
- ▶ Derive a mathematical model from the physics and the physical interaction.

$$\mathbf{g} = \mathcal{H}\mathbf{f}$$

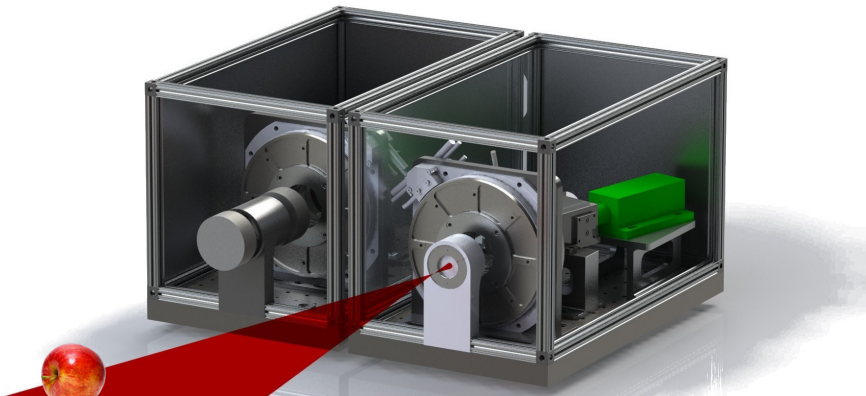


Working backward - inverting the model



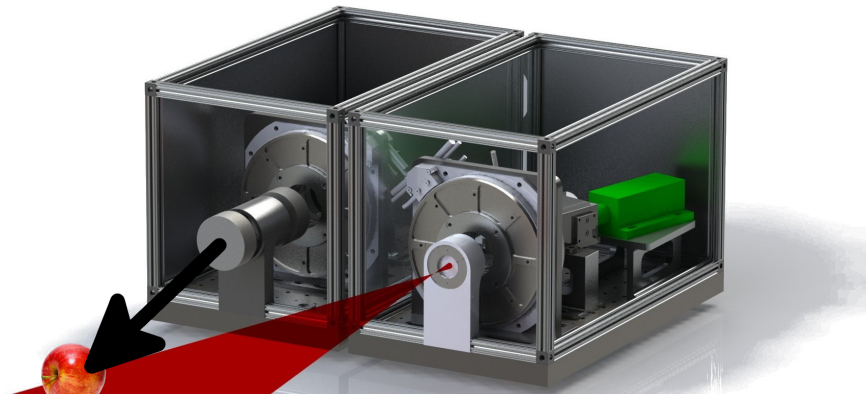
Working backward - inverting the model

- Begin with the model...



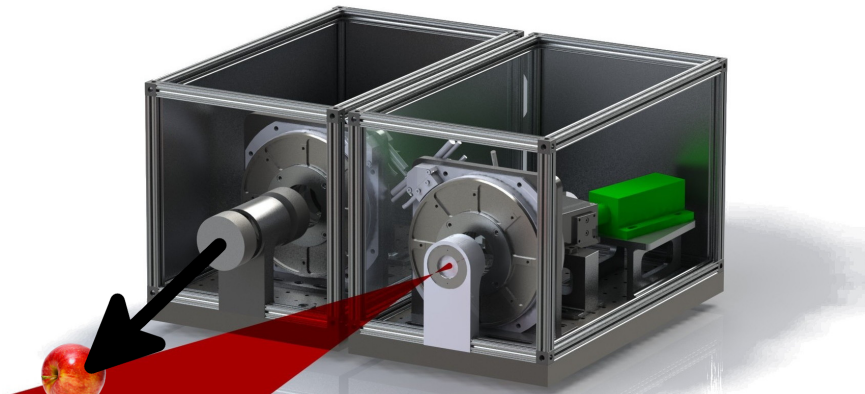
Working backward - inverting the model

- ▶ Begin with the model...
- ▶ Invert the model (work backwards) to obtain...



Working backward - inverting the model

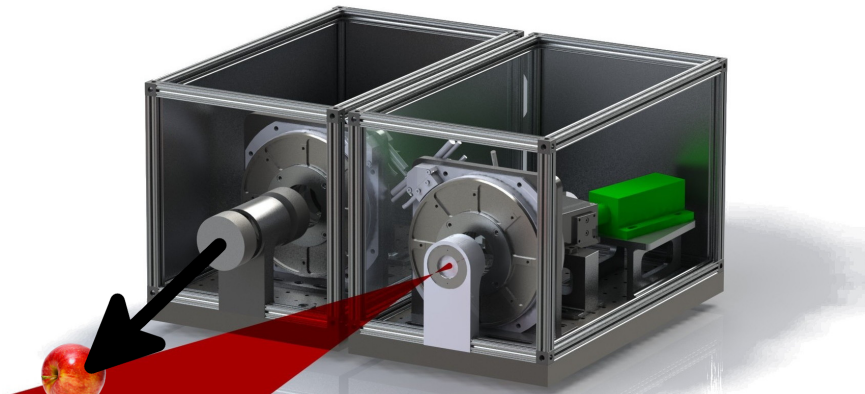
- ▶ Begin with the model...
- ▶ Invert the model (work backwards) to obtain...
- ▶ An estimation of the physical quantity.



Working backward - inverting the model

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- ▶ Invert the model (work backwards) to obtain...
- ▶ An estimation of the physical quantity.

$$\mathcal{H}^{-1}\mathbf{g} = \mathbf{f}$$

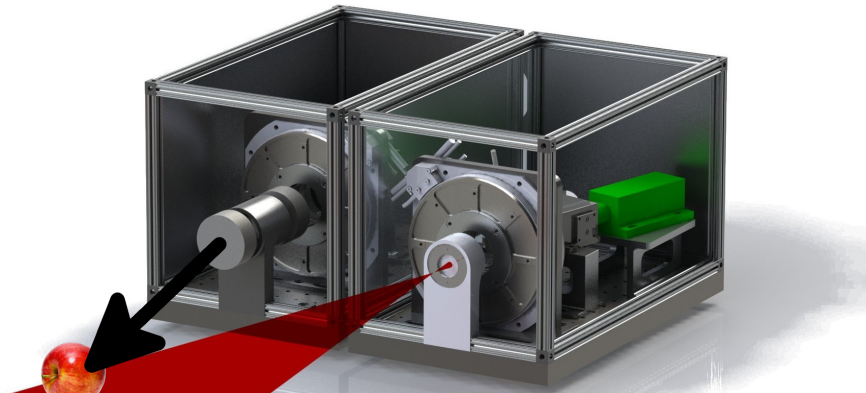


Working backward - inverting the model

- ▶ Begin with the model...
- ▶ Invert the model (work backwards) to obtain...
- ▶ An estimation of the physical quantity.

$$\mathcal{H}^{-1}\mathbf{g} = \mathbf{f}$$

Inverting the model is a subject of an entire mathematical subfield called *Stochastic or statistical estimation theory*.



Example : MRI

- ▶ 2003 Nobel prize in medicine awarded to Mansfield and Lauterbur.

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- ▶ Imaging science model developed by Mansfield.

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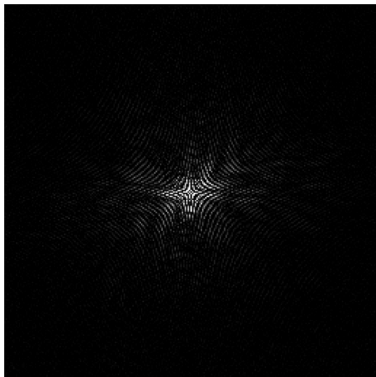


Figure 1: image

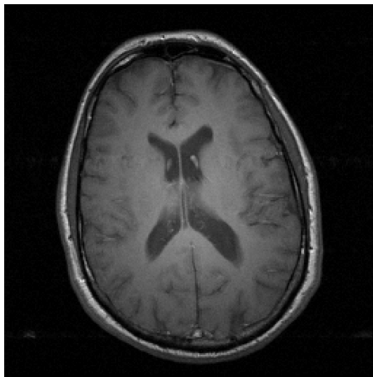
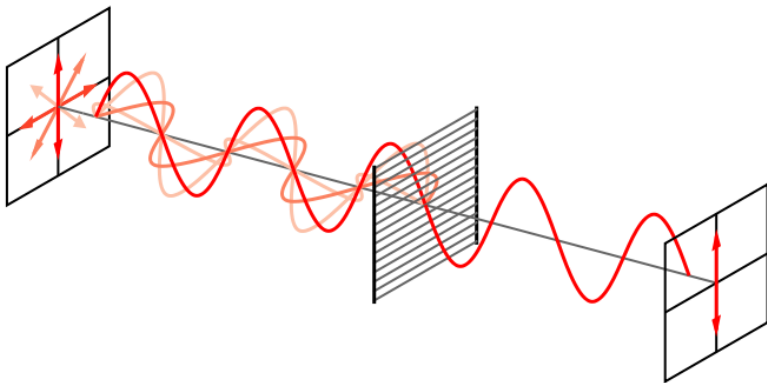


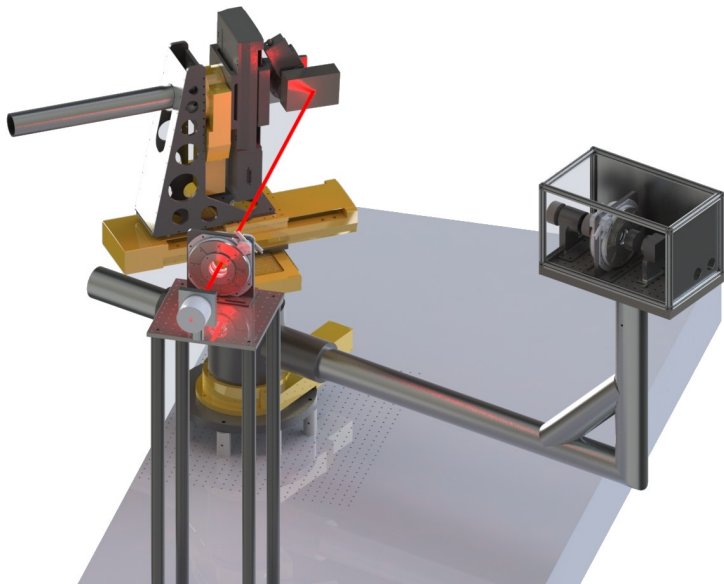
Figure 2: object

Oriented electric field



Electric field is oriented in space.

Polarimetric instrument

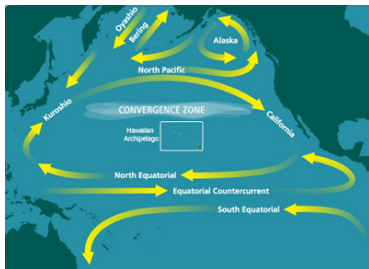


Polarimetric camera equation

$$\begin{aligned}
& \sum_{j'} \frac{\ell^2}{\mu_0 \omega_{j'}} \operatorname{Re} \left\{ \left[\left(e^{i\ell_{m,n} \cdot \kappa_{j'}} \operatorname{sinc} \left(\frac{\ell \kappa_{j'}}{2\pi} \right) * \mathcal{F}_2 \left\{ \mathcal{H}^2(\theta_{m,n}) \tilde{\mathbf{f}}(\mathbf{r}, 0) \right\} \cdot \tilde{\mathbf{e}}_{j'} \right) k_{z,j'} \right. \right. \\
& \quad \left. \left. - \left(\left[e^{i\ell_{m,n} \cdot \kappa_{j'}} \operatorname{sinc} \left(\frac{\ell \kappa_{j'}}{2\pi} \right) * \mathcal{F}_2 \left\{ \mathcal{H}(\theta_{m,n}) \tilde{\mathbf{f}}(\mathbf{r}, 0) \right\} \right] \cdot \kappa_{j'} \right) e_{z,j'} \right] \right\} \\
& + \sum_{j'} \frac{\ell^2}{\mu_0 \omega_{j'}} \operatorname{Re} \left\{ \left[\left(e^{-i\ell_{m,n} \cdot \kappa_{j'}} \operatorname{sinc} \left(\frac{\ell \kappa_{j'}}{2\pi} \right) * \mathcal{F}_2 \left\{ \mathcal{H}^2(\theta_{m,n}) \tilde{\mathbf{f}}^*(\mathbf{r}, 0) \right\} \cdot \tilde{\mathbf{e}}_{j'} \right) k_{z,j'} \right. \right. \\
& \quad \left. \left. - \left(\left[e^{-i\ell_{m,n} \cdot \kappa_{j'}} \operatorname{sinc} \left(\frac{\ell \kappa_{j'}}{2\pi} \right) * \mathcal{F}_2 \left\{ \mathcal{H}(\theta_{m,n}) \tilde{\mathbf{f}}^*(\mathbf{r}, 0) \right\} \right] \cdot \kappa_{j'} \right) e_{z,j'} \right] \right\}
\end{aligned}$$

Polarimetric instrument application

- Pacific plastic patch.



Polarimetric instrument application

- ▶ Pacific plastic patch.
- ▶ Plastic quantity completely unknown.

