

Solution to Practice for Exam 1.

1.

$$-\frac{1}{10}e^{-3t} \cos t + \frac{3}{10} \sin t e^{3t} + C.$$

2.

$$t - \sqrt{7} \arctan\left(\frac{t}{\sqrt{7}}\right) + C$$

3.

$$\arcsin\left(\frac{x+4}{\sqrt{2}}\right) + \left(\frac{x+4}{\sqrt{2}}\right) \sqrt{1 - \left(\frac{x+4}{\sqrt{2}}\right)^2} + C$$

4.

$$-\ln \left| \frac{1 + \sqrt{1 - \left(\frac{1}{1 + \left(\frac{x+2}{\sqrt{3}}\right)^2}\right)}}{1 - \sqrt{1 - \left(\frac{1}{1 + \left(\frac{x+2}{\sqrt{3}}\right)^2}\right)}} \right| + \sqrt{3} \sqrt{1 + \left(\frac{x+2}{\sqrt{3}}\right)^2} + C$$

5.

$$\frac{1}{2} \arcsin\left(2\left(x - \frac{1}{2}\right)\right) + C$$

6.

$$\frac{1}{2} \ln \left| \frac{1 + \sin y}{1 - \sin y} \right| + C$$

7.

$$2 \ln \left| \frac{t-4}{t-2} \right| + C$$

8.

$$2 \ln |u| - \ln |u^2 + 1| + C$$

9.

$$-5 \ln |x - 1| + 6 \ln |x - 2| + \frac{3}{x-1} + C$$

10.

$$\frac{2}{3}(x+1)^{\frac{3}{2}} - 2(x+1)^{\frac{1}{2}} + C$$

11.

$$0$$

12.

$$\frac{x^2}{2} + \frac{1}{2} \ln \left| \frac{x}{x+2} \right| + C$$

13.

$$\frac{\sin^3 y}{3} - \frac{\sin^5 y}{5} + C$$

14.

$$\frac{\sqrt{3}}{\sqrt{2}} \arcsin\left(\frac{\sqrt{2}x}{\sqrt{3}}\right) + C$$

15.

(a) $TRAP(2) = \frac{\sqrt{2}\pi}{8} + \frac{\pi}{8}$

(b) $MID(2) = \sin\left(\frac{\pi}{8}\right)\frac{\pi}{4} + \sin\left(\frac{3\pi}{8}\right)\frac{\pi}{4}$

(c) $SIMP(2) = \frac{\sin\left(\frac{\pi}{8}\right)\frac{\pi}{2} + \sin\left(\frac{3\pi}{8}\right)\frac{\pi}{2} + \frac{\sqrt{2}\pi}{8} + \frac{\pi}{8}}{3}$