

§1.10 Lines

$$Ax + Bx + C = 0$$

general

$$y = mx + b$$

slope intercept form

$$y - y_1 = m(x - x_1)$$

Point
Slope

$$m = \text{slope} = \frac{\text{rise}}{\text{run}} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{\Delta \text{output}}{\Delta \text{input}}$$

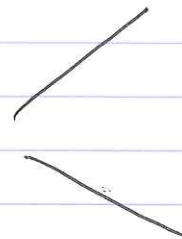
Special Cases:

$m = 0$ Horizontal line $y = \text{Constant}$

~~$m = \infty$~~ Vertical line $x = \text{Constant}$ (only lines which aren't functions)

$m > 0 \Rightarrow$ increasing line.

$m < 0 \Rightarrow$ decreasing line



parallel/perpendicular

Given

Two lines $L_1: y = m_1x + b_1$

$L_2: y = m_2x + b_2$

parallel $\parallel: m_1 = m_2$

perpendicular $\perp: m_1 = -\frac{1}{m_2}$

Practice:

1.) Find the equation of the line

(a) goes thru $\begin{matrix} A \\ (-1, 1) \end{matrix}, \begin{matrix} B \\ (3, 9) \end{matrix}$

$$m = \frac{9-1}{3-(-1)} = \frac{8}{4} = 2$$

$$y-1 = 2(x+1)$$

$$y = 2(x+1) + 1$$

$$\boxed{y = 2x + 3}$$

(b) perpendicularly bisects AB (as above)

$$m = -\frac{1}{m_1}$$

point? midpt: (avg of x, avg of y)

$$(1, 5)$$

$$m = -\frac{1}{2}$$

$$y-5 = -\frac{1}{2}(x-1)$$

$$\boxed{y = -\frac{1}{2}x + \frac{11}{2}}$$

(c) parallel to $3x + 2y = 5$ and goes thru $(1, 0)$

$$\rightarrow 2y = 5 - 3x$$

$$y = \frac{5}{2} - \frac{3}{2}x$$

$$m_1 = \frac{3}{2}$$

// same

$$m = -\frac{3}{2}$$

$$\Rightarrow y-0 = -\frac{3}{2}(x-1)$$

$$\boxed{y = -\frac{3}{2}x + \frac{3}{2}}$$

2.) # 65 on p 122

★ # 63

Algebra Test Results on Monday!

→ 1.7, 1.8 may be turned in on Monday

§ 1.9 (very brief overview)

CALCULATORS OUT!!

Main Features

1.) graphing functions.

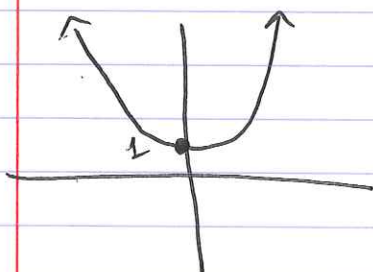
Practice:

Sketch $y = x^2 + 1$

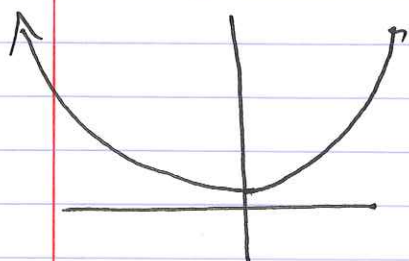
(a) in $[-10, 10] \times [-10, 10]$,

$\{$
x values

$\}$
y-values

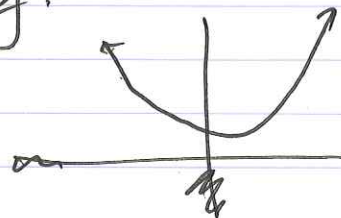


(b) in $[-5, 5] \times [-20, 20]$



observe, Q III, IV are empty.

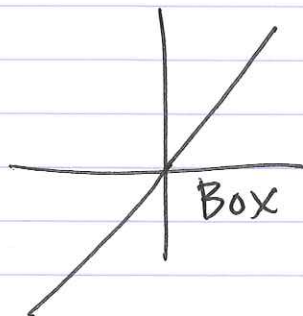
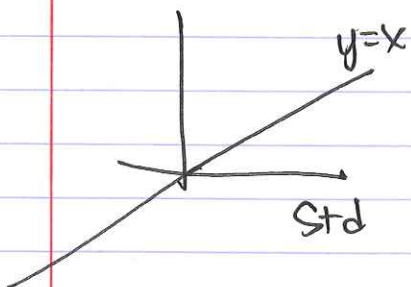
⇒ Set $y_{\min} \geq 0$.



"Shortcuts" to adjusting your window:

2.) Zoom feature.

1. ~~zbox~~ Zbox → makes a 1-1 scale
bit x and y-values



6: Z Standard

0: Zoomfit : autoadjust to attempt
to put entire graph
into view.

Example:

$$\text{Graph: } x^4(100-x^2)(x+50)=y$$

↳ zoomfit fails

(we know graph
should look
like an "S")

How can we improve
this window?

3.) Table + Our Brains

Table

↳ TBLSET

Window

Indep: Auto

↑

Calc fills
in x's

Ask

↑

user enters
in x's

Dep: ALWAYS set to Auto

You guys! (20 mins - turn in 1 sheet
per pair.)

x-

1.) Find the intercepts, rounded to 2
decimal places.

$$y = \sqrt{x} + x - x^2$$

2.) Solve the equation, " " " "

$$x^4 = x^3 - x^9$$

3.) Solve the inequality, " " " "

$$(x+1)^2 < (x-1)^2$$