

5.1

Radian measure

↙ ch6  
angle

↘ ch5

arclength on unit  
circle.  
↓  
 $r=1$

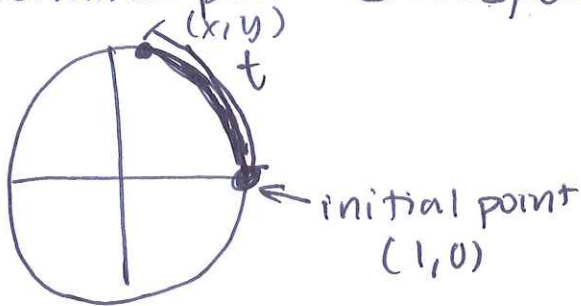
$$S = r\theta$$

on unit circle

$$S = \theta$$

Def

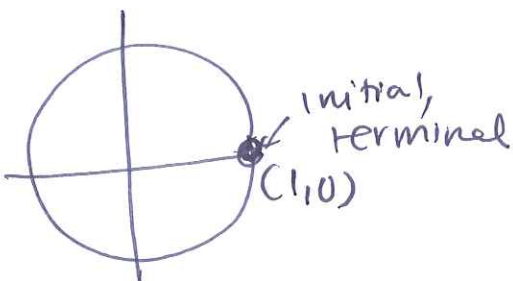
terminal point corresponding to  $t$ :



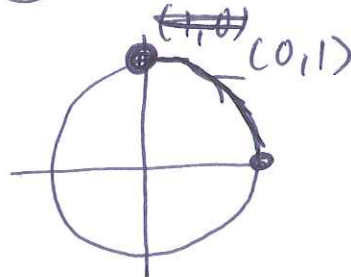
the point  $(x, y)$  that is  $t$  away from  $(1, 0)$  on the unit circle.

Example: Find ~~terminal point~~ terminal point corresponding to  $t$ .

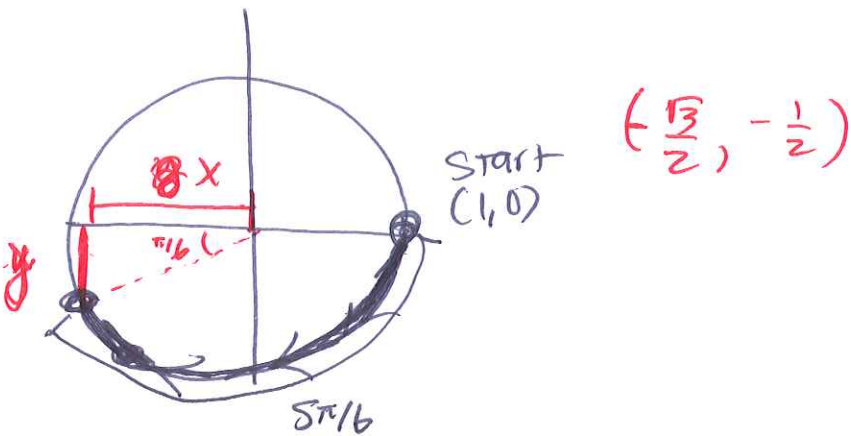
(a)  $t = 0$



(b)  $t = \pi/2$

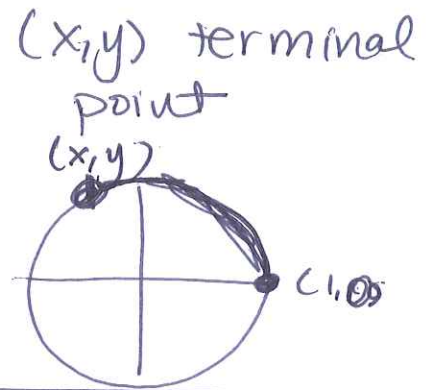


(c)  $t = -5\pi/6$



§5.2 Trig functions of real numbers

$\sin(t) = y$   
 $\cos(t) = x$   
 $\tan(t) = y/x$

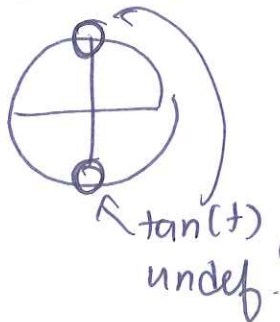


Domain:

$\sin(t) \neq (-\infty, \infty)$

$\cos(t) \neq (-\infty, \infty)$

$\tan(t) \neq x \neq 0$



$t \neq \pi/2, 3\pi/2, 5\pi/2, \dots$   
 $-\pi/2, -3\pi/2, \dots$

$t \neq \pi/2 + \pi k, k \text{ is an integer.}$

## Symmetries:

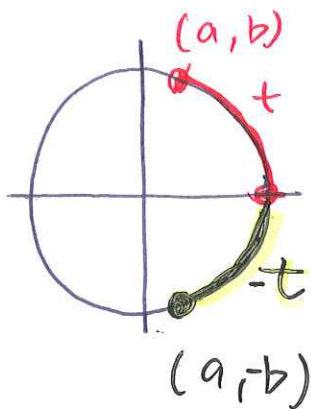
Even:  $f(-x) = f(x) \longleftrightarrow$  symm y axis

ODD:  $f(-x) = -f(x) \longleftrightarrow$  symm about origin.

## Example 2:

Q: Is  $\sin(t)$  even, odd or neither?

$$\sin(-t) = -b = -(b) = -\sin(t)$$



$\sin(t)$  is odd.  
(sym about origin)

Q: What about  $\cos(t)$ ?

$$\cos(-t) = a = \cos(t)$$

$\cos(t)$  is even  
(sym about y-axis)

Example 3: Using trig identities, determine if even, odd, neither

(a)  $\sec(t)$ .

$$\sec(-t) = \frac{1}{\cos(-t)} = \frac{1}{\cos t} = \sec(t)$$

$$\sec(-t) = \sec(t)$$

$\Rightarrow$  even.

(b)  $\csc(t)$ :

$$\csc(-t) = \frac{1}{\sin(-t)} = \frac{1}{-\sin(t)} = -\csc(t)$$

$\Rightarrow$  ODD.

(c)  $\tan(t)$ :

$$\tan(-t) = \frac{\sin(-t)}{\cos(-t)} = \frac{-\sin(t)}{\cos(t)} = -\tan(t)$$

$\Rightarrow$  ODD.

(d)  $\tan(t) + \sec(t)$ :

$$\tan(-t) + \sec(-t) = \underbrace{-\tan(t)}_{\text{opp}} + \underbrace{\sec(t)}_{\text{same}}$$

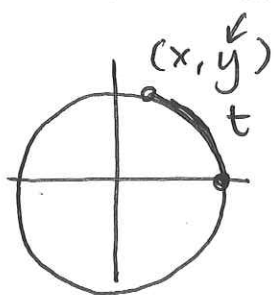
neither even nor odd

**5.3** Graphs of sine/cosine.

$y = \sin(t)$

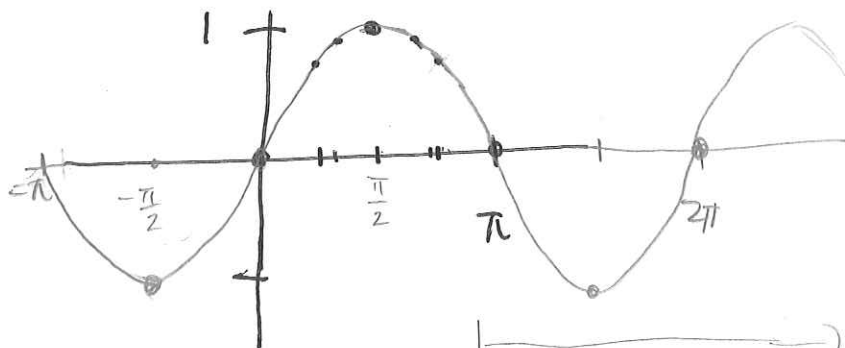
D:  $(-\infty, \infty)$

R:  $[-1, 1]$



vert value on circle!

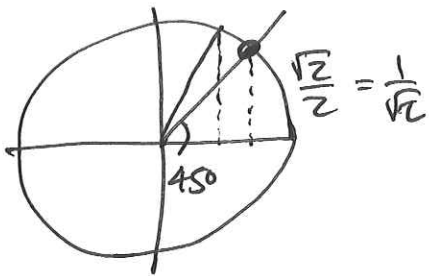
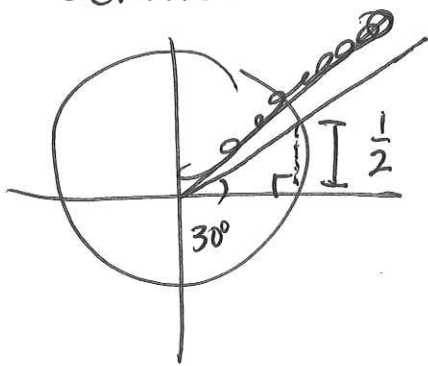
t	$\sin(t)$
0	0
$\pi/6$	$1/2$
$\pi/4$	$\sqrt{2}/2$
$\pi/3$	$\sqrt{3}/2$
$\pi/2$	1
$2\pi/3$	$\sqrt{3}/2$
$5\pi/6$	$1/2$
$\pi$	0
$2\pi$	0
$2\pi/3$	$\sqrt{3}/2$
$5\pi/6$	$1/2$
$\pi$	0
$7\pi/6$	$-1/2$
$3\pi/2$	-1
$5\pi/3$	$-\sqrt{3}/2$
$11\pi/6$	$-1/2$
$2\pi$	0



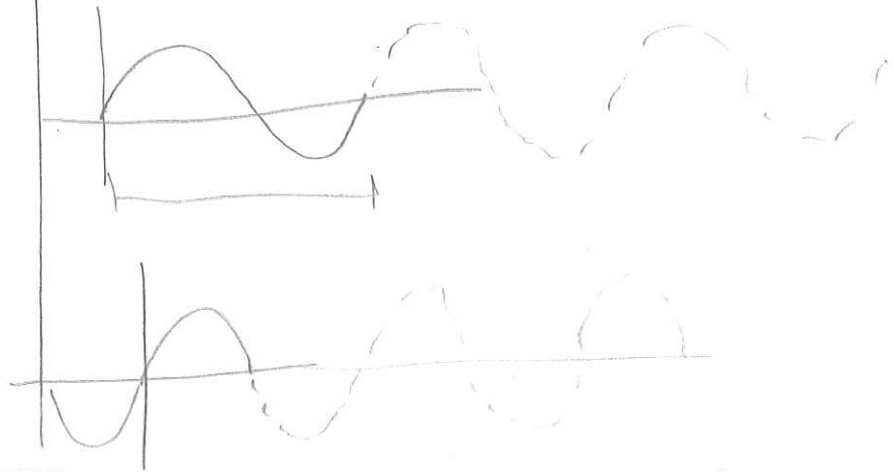
$\sin(-x) = -\sin x$

repeats!  
every  $2\pi$ .

Scratch



$\sin(t)$  is periodic.  
1 full cycle (pattern)  
can generate the entire graph.



width of cycle = period

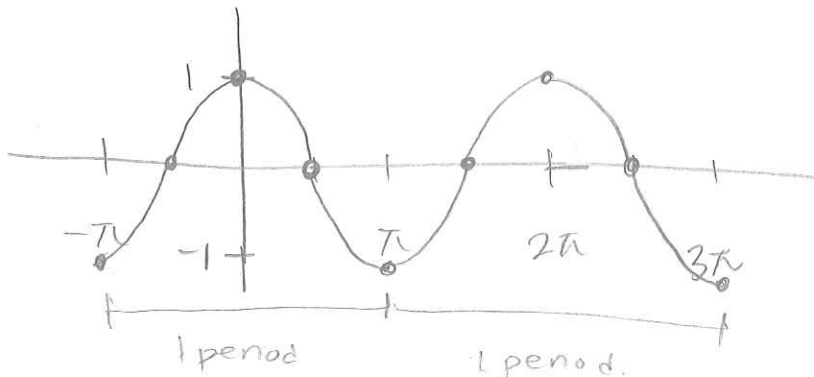
||  
the <sup>smallest</sup> number so that  
 $f(x+p) = f(x)$  for all  $x$ .

period of  $\sin(t)$ :  $2\pi$

amplitude: stretch away from middle.

amplitude 1.

$y = \cos(t)$



period:  $2\pi$

amp: 1

middle/avg:  $y=0$