

**Math 263 Section 005: Statistics and Bio-Statistics, Spring 2014**

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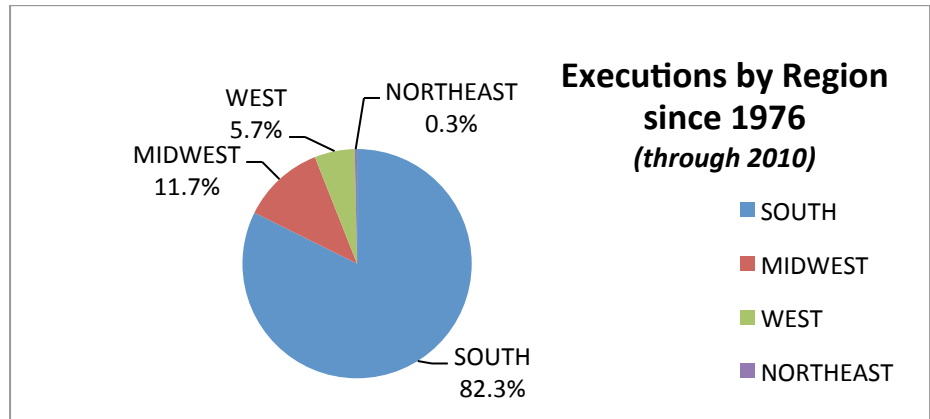
Course Policies and Information at <http://math.arizona.edu/~dh/263-14.html>. You will need a webassign account for the course. Go to [www.webassign.net](http://www.webassign.net). The class key is **Arizona 7989 8719**

Today’s class will cover graphs (bar graphs, pie charts, histograms) and numerical descriptors (mean, median, standard deviation, IQR). This is Sections 1.1, 1.2 in Introduction to the Practice of Statistics, 7-th edition, by D. Moore, G. McCabe, B. Craig. (W.H. Freeman, 2012)

**GRAPHS**

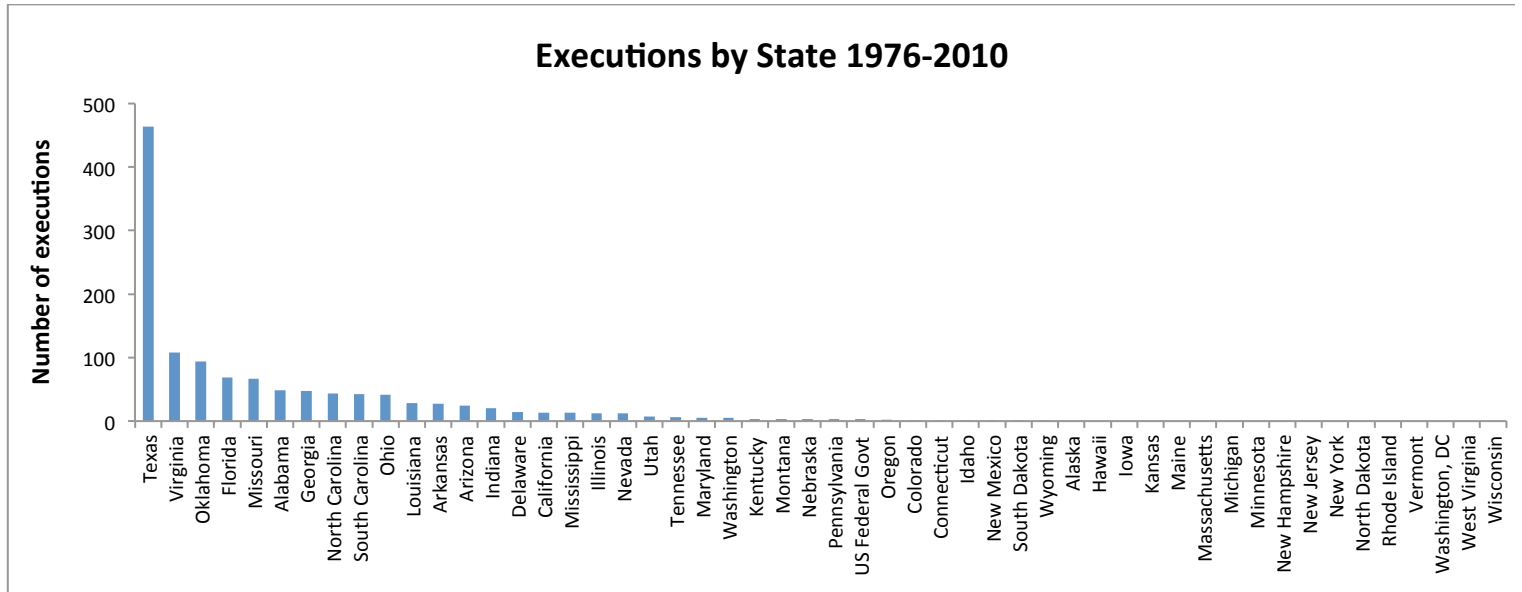
**Executions by Region**

REGION	TOTAL	
SOUTH	1016	0.823
MIDWEST	144	0.117
WEST	70	0.057
NORTHEAST	4	0.003
<b>Total</b>	<b>1234</b>	<b>1.000</b>



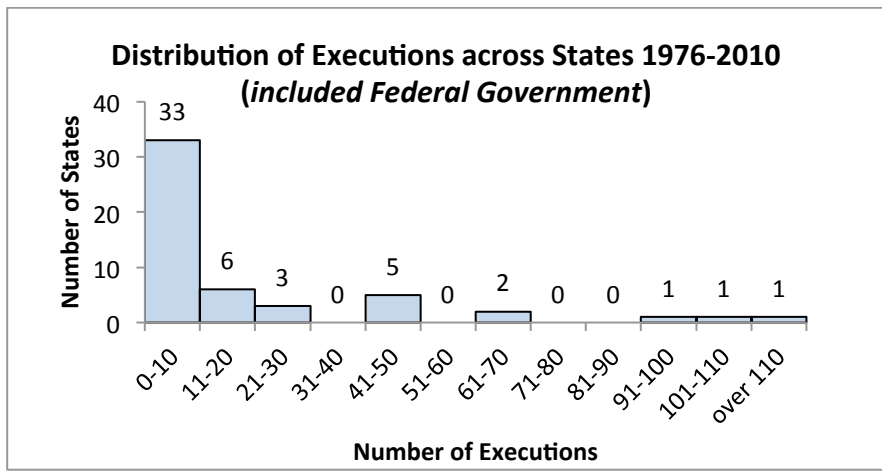
How would you make a pie chart?

**Executions by State** What sort of graph is this? What is it useful for?



**What is a histogram?** For the executions by state, make a count using the bins below, then make a bar chart:

Bin	Frequency
10 or less	33
20	6
30	3
40	0
50	5
60	0
70	2
80	0
90	0
100	1
110	1
More	1



From Death Penalty Information Center (<http://www.deathpenaltyinfo.org>)

STATE	TOTAL EXECUTIONS
Texas	464
Virginia	108
Oklahoma	94
Florida	69
Missouri	67
Alabama	49
Georgia	48
North Carolina	43
South Carolina	42
Ohio	41
Louisiana	28

Arkansas	27
Arizona	24
Indiana	20
Delaware	14
California	13
Mississippi	13
Illinois	12
Nevada	12
Utah	7
Tennessee	6
Maryland	5
Washington	5
Kentucky	3

Montana	3
Nebraska	3
Pennsylvania	3
US Federal Govt	3
Oregon	2
Colorado	1
Connecticut	1
Idaho	1
New Mexico	1
South Dakota	1
Wyoming	1
<b>Total</b>	<b>1234</b>

Also 17 states with no executions.

**Numbers that Describe the Distribution of the Data: “Sample Statistics”**

**Statistics including Texas**

Mean =  
 Median =  
 Standard Deviation =  
 Quartiles: Q1 =  
 Quartiles: Q2 =  
 Quartiles: Q3 =  
 IQR =

**Outliers with Texas**

1.5×IQR = above  
 Q3 and below Q1.  
 So above That is,

**Descriptors without Texas**

Mean =  
 Median =  
 Standard Deviation =  
 Quartiles: Q1 =  
 Quartiles: Q2 =  
 Quartiles: Q3 =  
 IQR =

**Outliers without Texas**

1.5×IQR = above  
 Q3 and below Q1.  
 So above That is,

### Statistics: Mean, Median, Standard Deviation

To communicate about a distribution without showing a histogram, *sample statistics* are useful.

Suppose the data values are  $x_1, x_2, x_3, \dots, x_n$ , so  $n$  is the size of the data set. Then  $x_i$  is a typical data value for  $i = 1, 2, \dots, n$ .

- **Mean**, or average value,  $\bar{x}$ , obtained by adding the values and dividing by the number of values.

$$\bar{x} = \frac{\sum_{i=1}^n x_i}{n} = \frac{x_1 + x_2 + \dots + x_n}{n}$$

- **Median** is the middle value. If there is an even number of values, the median is the average of the two middle values.
- **Standard Deviation** measures spread of the data:

$$s_x = \sqrt{\frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n - 1}}$$

Why take the square root?

Why is it  $(n - 1)$  and not  $n$ ?

On a histogram:

Mean is “balance point”

Median has half the data to the left, half to the right.

Standard deviation is “average distance from mean”

In Excel,

Mean is =AVERAGE(array);

Median is =MEDIAN(array);

Standard deviation is =STDEV(array) or STEV.S(array) in Excel 2010 and 2011

Ex: If data set is 1, 2, 9, 20, 5 then  $n = 5$  and the statistics are:

Why is the mean larger than the median?

What does the standard deviation represent?

### **What are can we learn from Sample Statistics ?**

1. Look at the relationship between the mean and the median: How does this relate to the shape of the graph?  
This histogram is called **skewed right** because the tail goes to the right.
2. Which of the statistics change a lot when Texas is removed? Why? These statistics are called **sensitive**, or said to be **not robust**.
3. Which statistics are robust?
4. What generalization can you make about outliers and the shape of the graph?

### **Box Plot**