

Name \_\_\_\_\_

Homework 13  
Section 14.6

1. (6) Find  $\frac{\partial z}{\partial u}$  and  $\frac{\partial z}{\partial v}$  for  $z = x^2 + 2xy$ ,  $x = \frac{u^2}{v}$ ,  $y = 2u + v$ .

2. (6) Let  $T(x, y) = 4x^2 - 4xy + 5y^2$ ,  $x = \cos t$ , and  $y = -\sin t$ ,  $0 \leq t < 2\pi$ . Compute  $\frac{dT}{dt}$ .

3. (8) If  $w = f(x, y)$ , where  $x = r \cos \theta$  and  $y = r \sin \theta$ , show that

$$\left(\frac{\partial w}{\partial x}\right)^2 + \left(\frac{\partial w}{\partial y}\right)^2 = \left(\frac{\partial w}{\partial r}\right)^2 + \frac{1}{r^2} \left(\frac{\partial w}{\partial \theta}\right)^2$$